

this is guessing questions for old session now we will provide all new questions in class

Index, "Get Free Formula Book (Red) From Our Office"

- Page: 1: Single Answer Type Questions (List 1)
- Page: 2: More than one may correct answer type que. (List 1)
- Page: 3: Integer (Four Digit) answer type que. (List 1)
- Page: 3: Single Answer type questions (List 2)
- Page: 4: Comprehension Type Questions (List 1)
- Page: 5: Match Matrix Type Questions.
- Page: 6: Integer (Four Digit) answer type que (List 2)
- Page: 6: Single Answer Type Questions (List 3)
- Page: 7: Comprehension type questions (List 2)
- Page: 7: More than one correct answer type (List 2)
- Page: 8: Single correct answer type que (List 4)
- Page: 9: Integer (Single Digit) type questions.
- Page: 10: Integer (Four Digit) type questions (List 3)
- Page: 11: Comprehension Type questions (List 3).
- Page: 12: Answer key: & VERY IMP MESSAGE

Time Table for Session 2013-2014

Maths by SUHAAG KARIYA

INDRAPURI (BHEL) C-69	Class 11 <sup>th</sup> : MON, WED, FRI; 4 pm to 6 pm
	Class 12 <sup>th</sup> : TUE, THU, SAT; 4 pm to 6 pm

SUNDAY : Text & Doubt Discussion

M.P. Nagar R-1, Zone 2.	Class 11 <sup>th</sup> : MON, WED, FRI; 6:30 pm to 8:30 pm
	Class 12 <sup>th</sup> : TUE, THU, SAT, 6:30 to 8:30 pm
CRASH COURSE FOR JEE MAIN Daily 8 am to 11 am	

MATHS

Sheet 1; Differential Calculus; F., L., C., D., MOD, AOD,  
It is final practice on MATHEMATICS for IIT JEE/AIEEE  
SINGLE CORRECT ANSWER TYPE (Q.1 to 7) (SUHAG SIR) 2012.

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Q.1. Which of the following equations have the same graph.

- I.  $y = x - 2$
- II.  $y = \frac{x^2 - 4}{x + 2}$
- III.  $(x + 2)y = x^2 - 4$

- (A) I & II only
- (B) I & III only
- (C) II & III only
- (D) All have different graphs.

Q.2. If  $\lim_{x \rightarrow -2} \frac{(2(a-3)(x+2) - 6\sin^{-1}(x+2))\tan^{-1}(5x+10)}{(x+2)^2} = 0$  then the value of "a" is equal to (WWW.TEKOCLASSES.COM) 10,12,1,1,2

- (A) 9
- (B) 6
- (C) 3
- (D) 12

Q.3. Let  $f(x) = 11 - 8\sin x - 2\cos^2 x$ . If the maximum & min. values of  $f(x)$  are denoted by M & m respectively then  $(M-1)/m$  has the value equal to: 10,12,1,1,4

- (A) 6
- (B) 18
- (C) 5
- (D) 0

Q.4. Let f be a real valued function defined on R given by  $f(x) = \{x\} + 2[x]$ ; where  $\{ \}$  FPF &  $[ ]$  GIF. Then f(x) is 10,12,1,1,5

- (A) Continuous & Differentiable at  $x \in R$
- (B) Continuous  $\forall x \in R$  but not differentiable at integral points
- (C) neither continuous nor derivable at integral points
- (D) No where differentiable. [Draw Graph Also]

Q.5. If the right hand derivative of  $f(x) = [x]\tan \pi x$  at  $x=7$  is  $k\pi$ , then k is equal to 10,12,1,1,6

- (A) 6
- (B) 7
- (C) -7
- (D) 49

Q.6. Let  $f(x) = \begin{cases} (\sin x + \cos x)^{\csc x} & ; -\frac{\pi}{2} < x < 0 \\ a & ; x = 0 \\ \frac{e^{\frac{1}{x}} + e^{\frac{2}{x}} + e^{\frac{3}{x}}}{ae^{\frac{2}{x}} + be^{\frac{3}{x}}} & ; 0 < x < \frac{\pi}{2} \end{cases}$  is continuous at  $x=0$  then  $a^2 + b^2 =$  10,12,1,1,8

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- (A)  $2e^2$
- (B)  $e^2 + e^{-2}$
- (C)  $e + e^{-1}$
- (D)  $\frac{2}{e^2}$

Q.7. Paragraph for question 7(a) & 7(b) www.tekoclasses.com

Consider a quadratic expression  $f(x) = tx^2 - (2t-1)x + (5t-1)$  www.tekoclasses.com

Q.7(a) If f(x) take both positive and negative values then t must lie in the interval  $p \rightarrow 0$ .

(A)  $(-\frac{1}{4}, \frac{1}{4})$  (B)  $(-\infty, -\frac{1}{4}) \cup (\frac{1}{4}, \infty)$  ~~WRONG~~

(C)  $(-\frac{1}{4}, \frac{1}{4}) - \{0\}$  (D)  $(-4, 4)$  10, 12, 1, 1, 12 & 13

Q.7(b); If  $f(x)$  is non negative  $\forall x \geq 0$  then  $t$  lies in the interval.

(A)  $[\frac{1}{5}, \frac{1}{4}]$  (B)  $[\frac{1}{4}, \infty)$  (C)  $[-\frac{1}{4}, \frac{1}{4}]$  (D)  $[\frac{1}{5}, \infty)$

More than one may correct (Q.8 to Q.12) 10, 12, 1, 1, 14 & 18

Que 8. Which of the following statement(s) is (are) correct?

(A) Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be defined as  $f(x) = \frac{e^x}{1 + e^{2x}}$

then  $f(c) = \frac{1}{4}$  for some  $c \in \mathbb{R}$ . [www.tekoclasses.com](http://www.tekoclasses.com)

(B) If  $f(a)$  &  $f(b)$  possesses opposite signs then there must exist at least one solution of the equation  $f(x) = 0$  in  $(a, b)$ .

(C) If the function  $y = f(x)$  is continuous at  $x = x_0$  such that  $f(x_0) \neq 0$ , then  $f(x) \cdot f(x_0) > 0 \forall x \in (x_0 - h, x_0 + h)$  where  $h$  is sufficiently small positive quantity.

(D) Let  $f$  be a real valued continuous function on  $\mathbb{R}$  and satisfying  $f(-x) - f(x) = 0 \forall x \in \mathbb{R}$ . If  $f(-5) = 5$ ;  $f(-2) = 4$ ;  $f(3) = -2$ ;  $f(0) = 0$  then the equation  $f(x) = 0$  has at least 5 real roots. [www.tekoclasses.com](http://www.tekoclasses.com)

Que 9. Let  $f(x) = \max. (\sin^{-1}x, \frac{3\pi}{4}, \cos^{-1}x) \forall x \in [-1, 1]$  then

(A)  $f(x)$  is not derivable at  $x = \frac{1}{\sqrt{2}}$  Ph(0755)3200000

(B)  $f(x)$  is discontinuous at  $x = \frac{1}{\sqrt{2}}$  maths by SUHAG

(C)  $f'(\frac{\pi}{4}) = \frac{3\pi}{4}$  (D)  $f(x)$  is continuous but not derivable at  $x = -\frac{1}{\sqrt{2}}$

Que 10. For an arbitrary function  $f$  with domain  $(-\infty, \infty)$ , define  $F(x) = f(x) + f(-x)$  and  $G(x) = f(x) - f(-x)$ . Which of the following MUST be an odd function?

(A)  $F+G$  (B)  $F \cdot G$  (C)  $\frac{F}{G}$  (D)  $G \circ G$  [www.tekoclasses.com](http://www.tekoclasses.com)

Que 11. Let  $f$  be a differentiable function satisfying  $f(x+y) = f(x) + f(y) + e^x \cdot y \forall x \in \mathbb{R}, y \in \mathbb{R}$  and  $f(1) = e - 2$ . Then which of the following statement(s) is (are) true?

(A)  $\lim_{x \rightarrow 0} \frac{f(x)}{x} = 0$  (B)  $\lim_{x \rightarrow 0} \frac{f(x)}{x^2} = \frac{1}{2}$

(C)  $\lim_{x \rightarrow 0} \left[ \frac{f(x) + x}{x} \right] = 1$  (D)  $\lim_{x \rightarrow 0} \left( \frac{f(x) - f(-x)}{x^3} \right) = \frac{1}{6}$

P.T.O.

Que:12: Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be defined as

$$f(x) = \begin{cases} \lim_{n \rightarrow \infty} \left( \frac{[x]}{1+n^2} + \frac{3[x]}{2+n^2} + \frac{5[x]}{3+n^2} + \dots + \frac{(2n-1)[x]}{n+n^2} \right); x \neq \frac{\pi}{2} \\ 1; x = \frac{\pi}{2} \end{cases}$$

where  $[y]$  denotes largest integer  $\leq y$ , then which of the following statement(s) is (are) correct?

- (A)  $f(x)$  is injective but not surjective. [www.tekoclasses.com](http://www.tekoclasses.com)  
 (B)  $f(x)$  is not derivable at  $x = \frac{\pi}{2}$ .  
 (C)  $f(x)$  is discontinuous at all integer and cont. at  $x = \frac{\pi}{2}$ .  
 (D)  $f(x)$  is unbounded function. [www.tekoclasses.com](http://www.tekoclasses.com)

following two <sup>13&14</sup> questions are integer ans type (Upto 4 digits)

Q.13. Let  $g(x) = \begin{cases} a\sqrt{x+2}; 0 < x < 2 \\ bx+2; 2 \leq x \leq 5 \end{cases}$  If  $g(x)$  is derivable

on  $(0,5)$ , then find  $(2a+b)$ . Maths by SUHAG KARIYA

Q.14. For any real number  $x$ , let  $[x]$  denotes the largest integer less than or equal to  $x$ . Let  $f$  be a real valued function defined on the interval  $[-3,3]$  by  $f(x) = \begin{cases} -x - [x] & \text{if } [x] \text{ is even} \\ x - [x] & \text{if } [x] \text{ is odd} \end{cases}$

If  $L$  denotes the number of points of discontinuity and  $M$  denotes the number of points of non-derivability of  $f(x)$ , then  $(L+M)$ .

Single Correct Type

Que 15. Let  $f: (1, \infty) \rightarrow (0, \infty)$  be a continuous decreasing function with  $\lim_{x \rightarrow \infty} \frac{f(4x)}{f(8x)} = 1$  Then  $\lim_{x \rightarrow \infty} \frac{f(6x)}{f(8x)}$  is equal to (A)  $\frac{4}{8}$  (B)  $\frac{4}{6}$  (C)  $\frac{6}{8}$  (D) 1.

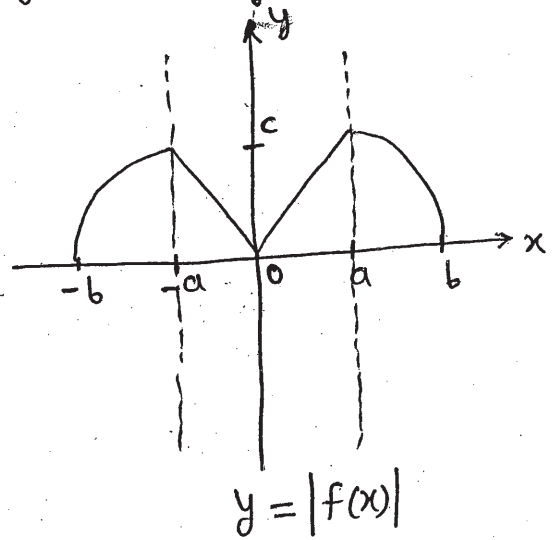
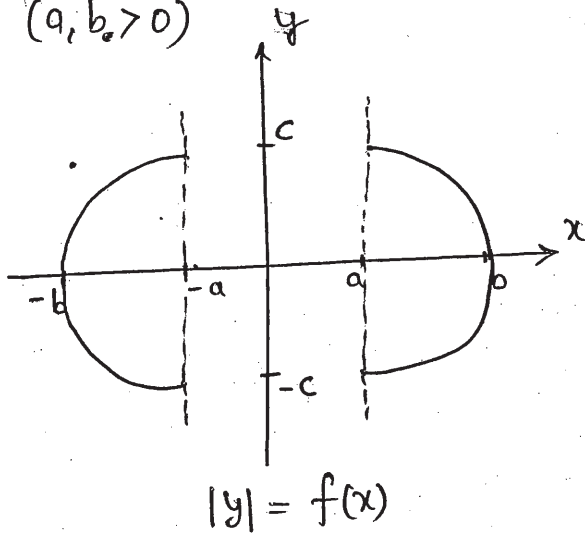
Que 16. The locus of the foot of the perpendicular from the origin upon chords of the circle  $x^2 + y^2 - 2x - 4y - 4 = 0$ , which subtends a right angle at the origin is.

- (A)  $x^2 + y^2 - x - 2y - 2 = 0$  (B)  $2(x^2 + y^2) - 2x - y + 3 = 0$   
 (C)  $x^2 + y^2 - 2x - 4y + 4 = 0$  (D)  $x^2 + y^2 + x + 2y - 2 = 0$

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Ques 17: If the graphs of  $|y|=f(x)$  &  $y=|f(x)|$  are given as below ( $a, b > 0$ )



Then identify the correct statement

- (A)  $f(x)$  is discontinuous at 2 points in  $[-b, b]$  and non-differentiable at 2 points in  $(-b, b)$
- (B)  $f(x)$  is discontinuous at 2 points in  $[-b, b]$  and non-differentiable at 3 points in  $(-b, b)$
- (C)  $f(x)$  is discontinuous at 3 points in  $[-b, b]$  and non-differentiable at 3 points in  $(-b, b)$
- (D)  $f(x)$  is discontinuous at 3 points in  $[-b, b]$  and non-differentiable at 3 points in  $(-b, b)$

Que 18, 19, 20 are on based upon this Paragraph 10, 12, 1, 2, 7, 8, 9

COMPREHENSION

Let  $f(x) = f_1(x) - 2f_2(x)$  where  $f_1(x) = \begin{cases} \min.(x^2, |x|); & -1 \leq x \leq 1 \\ x^2 & ; |x| > 1 \end{cases}$

&  $f_2(x) = \begin{cases} |x|; & |x| > 1 \\ \max(x^2, |x|); & |x| < 1 \end{cases}$  also

$g(x) = \begin{cases} \min. \{f(t); -3 \leq t \leq x, \text{ for } -3 \leq x < 0\} \\ \max. \{f(t); 0 \leq t \leq x, \text{ for } 0 \leq x < 3\} \end{cases}$  www.tekoclasses.com.

- Q.18 Range of  $f(x)$  (A)  $(-\infty, -1]$  (B)  $(-\infty, 1]$  (C)  $[1, \infty)$  (D)  $[-1, \infty)$
- Q.19 Number of values of  $x$  where  $g(x)$  fails to be differentiable is (A) 0 (B) 1 (C) 2 (D) 3
- Q.20.  $\lim_{x \rightarrow 0} f(g(x))$  is equal to (A) 0 (B) 1 (C) -1 (D) Non-existent.

Que 21. Match Matrices Type

10, 12, 1, 2, 1, 2

Column - I

COLOUMN II

- (A) If  $\lim_{x \rightarrow 3} \frac{f(x)-3}{x-2} = 1$  then  $\lim_{x \rightarrow 3} f(x)$  equals. (P) 15  
www.tekoclasses.com
- (B) A polynomial  $P(x)$  has remainder of 2, -13, 5 respectively when divided by  $(x+1)$ ,  $(x-4)$  &  $(x-2)$ . If the remainder when  $P(x)$  is divided by  $(x+1)(x-4)(x-2)$  is  $r(x)$ , then the value of  $r(1)$  is. (Q) 11  
maths by suhag
- (C) Consider the graphs of  $y = \sin x$ ,  $y = \cos x$ ,  $y = \tan x$ ,  $y = \cot x$ ,  $y = \sec x$  and  $y = \operatorname{cosec} x$  (R) 8  
Ph (0755) 3200000
- Let  $R = \left\{ (x, y) / 0 \leq x \leq \frac{\pi}{2}, 0 \leq y \leq 100 \right\}$ .  
 Number of points of  $R$  which lie on at least two of the graphs, is (S) 7
- (D) Suppose that  $2 - \sqrt{5}$  is a root of  $x^2 + Tx + b = 0$  where  $b$  is negative real number and  $T$  is an integer. The largest possible value of  $T$  is. (T) 4

Que 22 Column I

Column II

- (A) The number of points of non derivability of function  $f(x) = \left[ \frac{2x}{\pi} \right] \operatorname{sgn} \left( \frac{1}{\{x\}} \right)$  in  $(-2, 2)$  is (P) 2  
(where  $[y]$ ,  $\{y\}$  and  $\operatorname{sgn}(y)$  denotes largest integer  $\leq y$ , fractional part of  $y$  and signum func. of  $y$  respectively.)
- (B) The number of points of discontinuity of the function  $f(x) = \lim_{n \rightarrow \infty} \frac{(2 \sin x)^{2n}}{3^n - (2 \cos x)^{2n}}$ , is (Q) 3  
Maths by SUHAG KARIYA
- (C) Let ABC be a variable triangle such that A is  $(1, 2)$ , B & C lie on the line  $y = x + \lambda$  (R) 4  
(where  $\lambda$  is a variable). The locus of the orthocentre of triangle ABC is a straight line whose y intercept is equal to. (S) 5  
www.tekoclasses.com
- (D) The num of values of  $x$  satisfying  $\frac{\left( 2^{\frac{1}{x-1}} - 4 \right) (x-4)(x-9)}{|x - |(x-1)|} < 0$ , is (T) more than 5  
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Que 23 and Q. 24 are subjective, means there answer in 4 digit. <sup>10,12,12,1,3</sup>

Q.23. Let  $f(x) = \lim_{\theta \rightarrow 0} \frac{\cos(x+4\theta) - 4\cos(x+3\theta) + 6\cos(x+2\theta) - 4\cos(x+\theta) + \cos x}{\theta^4}$  www.tekoclasses.com

then find the absolute value of difference between maximum & minimum value of  $f(x)$ .

Q.24. of  $f(x) = \begin{cases} \frac{\sin [1x] \pi}{ax^4} + ax^2 + b; & -2 \leq x < -1 \\ 3 \sec \pi x + \cot^{-1} x & ; -1 \leq x \leq -\frac{3}{4} \end{cases}$

is differentiable in  $(-2, -\frac{3}{4})$  then  $a = \frac{1}{\lambda_1}$  and  $b = \frac{3\pi - \lambda_2}{4}$

find the value of  $(\lambda_1 + \lambda_2)$

Note:  $[y]$  denotes largest integer  $\leq y$ .

single ans. correct type

Q.25. Let  $\alpha$  be a real number such that  $0 \leq \alpha \leq \pi$ .

If  $f(x) = \cos x + \cos(x+\alpha) + \cos(x+2\alpha)$  takes some constant number  $c$  for any  $x \in \mathbb{R}$ , then the value of  $[c + \alpha]$  is equal to. (Not  $[.]$  is G.I.F.) Ph(0755)3200000

- (A) 0 (B) 1 (C) -1 (D) 2

Q.26. The line  $L_1$ , given by  $\frac{x}{5} + \frac{y}{b} = 1$  passes through the point  $M(13, 32)$ . The line  $L_2$  is // to  $L_1$  and has the equation  $\frac{x}{c} + \frac{y}{3} = 1$ . Then the distance between  $L_1$  &  $L_2$  is. Maths by SUHAAG KARIYA

- (A)  $\sqrt{17}$  (B)  $\frac{17}{\sqrt{15}}$  (C)  $\frac{23}{\sqrt{17}}$  (D)  $\frac{23}{\sqrt{15}}$

Q.27. Let  $g: \mathbb{R} \rightarrow \mathbb{R}$  be a differentiable function such that  $g(2) = -40$  and  $g'(2) = -5$ .

Then  $\lim_{x \rightarrow 0} \left( \frac{g(2-x^2)}{g(2)} \right)^{\frac{4}{x^2}}$

- (A)  $e^{32}$  (B)  $\sqrt{e}$  (C)  $1/\sqrt{e}$  (D)  $e^{-5}$  P.T.O.

Q.28. If 6, 8 and 12 are  $l^{\text{th}}$ ,  $m^{\text{th}}$  and  $n^{\text{th}}$  terms of an A.P. and  $f(x) = nx^2 + 2lx - 2m$ , then the equation  $f(x) = 0$  has

- (A) a root between 0 and 1 (B) both roots imaginary  
(C) both roots negative (D) both roots greater than 1.

Paragraph for question nos. 29 to 31. 10, 12, 2, 1, 6 to 8

Let  $f(x)$  be a polynomial function of degree 2

satisfying  $\int \frac{f(x)}{x^3 - 1} dx = \ln \left| \frac{x^2 + x + 1}{x - 1} \right| + \frac{2}{\sqrt{3}} \tan^{-1} \left( \frac{2x + 1}{\sqrt{3}} \right) + C$

where  $C$  is indefinite integration constant.

Q.29. The value of  $f(1)$  is equal to

- (A) 1 (B) 2 (C) -1 (D) -3

Q.30.  $\int \frac{1 - 6 \operatorname{cosec} x}{6 + f(\sin x)} d(\sin x) = g(x) + K$ , where  $g(x)$

contains no constant term.

Then  $\lim_{t \rightarrow \frac{\pi}{2}} g(t)$  is equal to (where  $K$  is integration constant)

- (A)  $\ln 1$  (B)  $\ln 2$  (C)  $\ln 3$  (D)  $\ln 4$

Q.31. Let  $\int \frac{5 + f(\sin x) + f(\cos x)}{\sin x + \cos x} dx = h(x) + \lambda$

where  $h(1) = -1$ , ( $\lambda$  is integration constant)

The value of  $\tan^{-1}(h(2)) + \tan^{-1}(h(3))$  is equal to

- (A)  $\frac{\pi}{4}$  (B)  $-\frac{\pi}{4}$  (C)  $\frac{3\pi}{4}$  (D)  $-\frac{3\pi}{4}$

More than one answer may correct (Q.32 to Q.35) 10, 12, 2, 1, 9 to 12

Q.32 which of the following limit vanishes?

- (A)  $\lim_{x \rightarrow 0^+} (x^{x^x} - x^x)$  (B)  $\lim_{x \rightarrow 0^+} x^2 \cdot \ln \sqrt{1/x}$  (C)  $\lim_{x \rightarrow 0^+} x^{\ln(x+1)}$   
(D)  $\lim_{x \rightarrow 0} (10^x - 2^x - 5^x + 1^x) / (x + \tan x)$

P.T.O.



Q.33. which of the following statement (s) is(are) always correct?

- (A) If  $f(x) > 1 \quad \forall x \in \mathbb{R}$  and  $\lim_{x \rightarrow 0} f(x)$  exist then  $\lim_{x \rightarrow 0} f(x) > 1$ .
- (B) There exist a function  $f$  defined on  $\mathbb{R}$  which is discontinuous  $\forall x \in \mathbb{R}$  but  $|f|$  is continuous  $\forall x \in \mathbb{R}$ .
- (C) Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be an even degree polynomial function then  $f$  is neither injective nor surjective.
- (D) Let  $f$  be a function defined on the set of all real numbers such that  $\lim_{x \rightarrow 0} \frac{f(x)}{x} = L$  (exists) and  $f(0) = 0$  then  $f$  is differentiable at  $x = 0$  and  $\lim_{x \rightarrow 0} f(x) = 0$

Q.34. Let  $f: \mathbb{R} \rightarrow [0, 1]$  be defined as  $f(x) = \cos(\sin x)$  then which of the following is (are) correct?

- (A)  $f$  is periodic with fundamental period  $2\pi$ .
- (B) Range of  $f = [\cos 1, 1]$
- (C)  $\lim_{x \rightarrow \frac{\pi}{2}} (f(\frac{\pi}{2} - x) + f(\frac{\pi}{2} + x)) = 2$
- (D)  $f$  is neither even nor odd function.

Q.35. If the equation  $\sin^2 \theta - a \sin \theta + b = 0$  has only one solution in  $(0, \pi)$ , then

- (A)  $a \in (-\infty, 1] \cup [2, \infty)$       (B)  $b \in (-\infty, 0] \cup [1, \infty)$
- (C)  $a = 1 + b$       (D)  $a + b = 1$

SINGLE CORRECT ANS. TYPE

Q.36

10, 12, 21, 1, C.

Let  $f(x) = \lim_{t \rightarrow 0} \frac{1}{t} \left( \tan^{-1} \left( \frac{1}{x+t} \right) - \tan^{-1} \left( \frac{1}{x} \right) \right)$

then absolute value of  $f(0)$  equals to

- (A) 4      (B) 1      (C) 6      (D) 7

P.T.O.

Q.37. If  $\lim_{x \rightarrow 0} \frac{1 - (1 - \sin x)(1 - \sin 2x) \dots (1 - \sin 100x)^{100}}{x(67670)} = k$

then the value of k, is equal to 10, 12, 2, 1, 2, C

- (A) 3 (B) 5 (C) 40 (D) 10 (E) 13

Q.38. Let  $\int \frac{(e^{2x} - e^x)}{(e^x + 1)\sqrt{e^{3x} + e^{2x} + e^x}} dx = 2 \tan^{-1}(\sqrt{f(x)}) + C$

where  $f(0) = 3$ . The minimum value of  $f(x)$  is equal to (where C is indefinite integration constant)

- (A) 3 (B) 5 (C) 40 (D) 10 (E) 13 10, 12, 2, 1, 2, D

Q.39. Let  $f(x) = \frac{\tan x}{x}$  and  $\lim_{x \rightarrow 0} ([f(x)] + x^2)^{\frac{1}{\{f(x)\}}} = e^L$

then L equals to (Note [ ] is GIF & { } is FPF)

- (A) 1 (B) 2 (C) 3 (D) 4 (E) 5

Q.40. Number of integers in the range of function

$f(x) = \sin(\sin^{-1}[x]) + \cos^{-1}(\cos[x])$  is equal to

- (Note [x] is GIF of x) (A) 1 (B) 2 (C) 3 (D) 4 (E) 5

single integer Answer type (Q.41 to 43) 10, 12, 2, 2, 1, 6, 6

Q.41. If the primitive of the function  $f(x) = \frac{\sin^4 x}{\cos^2 x}$  with respect to x is  $\tan x + g(x) + c$  where  $g(0) = 0$  and C is a constant of integration, then find the value of  $g\left(\frac{\pi}{8}\right) + g\left(\frac{\pi}{12}\right)$ .

Q.42. If a curve is represented parametrically by the equation

$$x = \sin\left(t + \frac{7\pi}{12}\right) + \sin\left(t - \frac{\pi}{12}\right) + \sin\left(t + \frac{3\pi}{12}\right),$$

$$y = \cos\left(t + \frac{7\pi}{12}\right) + \cos\left(t - \frac{\pi}{12}\right) + \cos\left(t + \frac{3\pi}{12}\right)$$

then find the value of  $\frac{d}{dt} \left( \frac{x}{y} - \frac{y}{x} \right)$  at  $t = \frac{\pi}{8}$ . P.T.O.

Q.43. see next Page

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Q.43. Let  $f(x) = \frac{\pi}{4} + \cos^{-1}\left(\frac{x}{\sqrt{1+x^2}}\right) - \tan^{-1}x$  and  $a_i$  ( $a_i < a_{i+1}$ ;  $\forall i=1, 2, 3, \dots, n$ ) be the positive integral values of  $x$  for which  $\text{sgn}(f(x))=1$ . Then find  $\sum_{i=1}^n a_i^2$ .

Four digit integer [0000 to 9999] answer type [Q.44 to Q.47]  
10, 12, 2, 2, 1 to 6

Q.44. Let  $f(x) = \begin{cases} a \cot^{-1}\left(\frac{b+x}{4}\right), & -\frac{2}{3} < x < 0 \\ 2, & x = 0 \\ \frac{\ln(1-cx)}{x}, & 0 < x < \frac{2}{3} \end{cases}$

If the function  $f(x)$  is differentiable at  $x=0$ , then find the value of  $(b^2 - 2a + c^6)$ .

Q.45. If the equation of tangent drawn to the curve  $y=f(x)$  at its points  $P(3, 5)$  is  $5x - 4y + 5 = 0$  and  $\lim_{x \rightarrow 3} \frac{(3^{4f(x)} - 2(1+3+3^2+\dots+3^{19}) - 1)^2}{1 - \cos(\ln(4-x))} = 2(a \cdot 3^b \cdot \ln c)^2$

where  $a, b, c$  are prime numbers and  $b \in \mathbb{N}$ , then find the value of  $(a+b+c)$ . Hint  $\cos \frac{\theta}{2} \cdot \cos \frac{\theta}{2} \cdot \cos \frac{\theta}{2} \dots$

Q.46. Let  $L = \lim_{n \rightarrow \infty} \frac{1}{\frac{1}{\sqrt{2}} \sqrt{\frac{1}{2} + \frac{1}{2} \sqrt{\frac{1}{2}}} \sqrt{\frac{1}{2} + \frac{1}{2} \sqrt{\frac{1}{2} + \frac{1}{2} \sqrt{\frac{1}{2}}} \dots n \text{ term}}}$

then find the value of  $(2\sqrt{3} \cot L)$

Q.47. Suppose  $\int \frac{1 - 7\cos^2 x}{\sin^7 x \cdot \cos^2 x} dx = \frac{g(x)}{\sin^7 x} + C$

where  $C$  is arbitrary constant of integration. Then find the value of  $g'(0) + g''\left(\frac{\pi}{4}\right)$ .

P.T.O.

Single Correct Answer Type:

Q.48. If the function  $f(x) = 2 \tan x + (2a+1) \ln |\sec x| + (a-2)x$  is increasing in  $(0, \frac{\pi}{2})$  then range of 'a' is equal to  
(A)  $(-\infty, 0]$  (B)  $[0, 1]$  (C)  $[0, 3]$  (D)  $[0, \infty)$

Q.49. If  $\ln(3 \sin x - 4 \cos x + 7 + 5y) = (\sin^2 x)y$ , then  $y'(\pi)$  is equal to.

(A)  $\frac{5}{3}$  (B) 0 (C)  $\frac{3}{5}$  (D)  $-\frac{3}{5}$  (E) -2.

Q.50. Let  $f: [0, 1] \rightarrow \mathbb{R}$  be a differentiable function with  $f(0) = 0$ , then  $\lim_{n \rightarrow \infty} n^2 \int_0^{\frac{1}{n}} f(t) dt$  equals

(A) 0 (B)  $\frac{1}{2} f'(0)$  (C)  $f'(0)$  (D)  $2 f'(0)$ .

Q.51. Let  $f(x) = [\tan x \cot x]$ ;  $x \in [\frac{\pi}{12}, \frac{\pi}{2})$ ;  $[ ] \rightarrow \text{G.I.F}$  where  
Then number of points, where  $f(x)$  is discontinuous is equal to

(A) One (B) Zero (C) three (D) Infinite

Q.52. Paragraph for questions Q.52 & Q.53

Let C be the curve  $f(x) = \ln^2 x + 2 \ln x$  and  $A(a, f(a))$   $B(b, f(b))$  where  $(a < b)$  are the points of tangency of two tangents drawn from origin to the curve C.

Q.52. The value of the product "ab" is equal to:

(A) e (B)  $\frac{1}{e}$  (C)  $e^2$  (D) 1

Q.53. Number of values of x satisfying the equation  $5x f'(x) - x \ln 10 - 10 = 0$  is equal to

(A) 0 (B) 2 (C)  $\infty$  (D) 1

इस sheet के हर प्रश्न को आप स्वयं, copy-pen से solve करें, और वस मेहनत करें आपका Selection हो ही गया समझें।

इसी तरह Next Sheets भी करें All The Best.

from SUHAAG SIR.

ANSWER KEY

- 1(D) 2(B) 3(A) 4(C) 5(B) 6(B) 7(a→C) 7(b→D) 8(ACD)  
9(CD) 10(BCD) 11(AB) 12(CD) 13(0003) 14(0012) 15(D)  
16\_\_\_\_. 17(B) 18(D) 19(C) 20(D) 21(A→T, B→\_\_\_\_, C→Q, D→\_\_\_\_)  
22 (A→Q, B→T, C→Q, D→R), 23(0002), 24(0017 not confirm)  
25(D) 26(C) 27(C) 28(A) 29\_\_\_\_, 30\_\_\_\_, 31\_\_\_\_,  
32 BD, 33 BCD, 34 BC, 35 ABC, 36 B, 37 B, 38 A  
39 C, 40 B, 41(0001), 42(0008), 43(0005), 44(0048)  
45(0028), 46(0000) 47\_\_\_\_, 48(D), 49(C), 50(B),  
51(C), 52(D), 53(B).

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Dear Students, इस sheet को आप घर पर इमानदारी से 1 hour में starting से solve करना शुरू करें (as exam hall) अभी बार बार Answer न देखें, और solve करते समय भी न देखें.

आप चेक करें आपने 1hr में कितने Questions पढ पाए ? कितने solve किए ? कितने Attemp किए ? फिर अपने Answer match करें. सही Ans पर +3 & Wrong Ans पर -1 Marks ले. अपने Final Marks देखें.

आपको IIT JEE (Main/Advanced) में भी एक subject का 1hr मिलेगा और ये sheet Present JEE Exam level की ही है.

ध्यान रहे कि IIT JEE 2010 के I Paper में 28 que<sup>on</sup> each subject पर आए थे, याने आपको इस level के 1hr में 28 que Attemp करने की Capability तो minimum होनी चाहिए.

इस प्रकार की सभी Topics पर sheets मेरे यहा Crash Course (starting from 21 March Daily 8am to 11pm) में करवाई जाएगी.

तो समय का उपयोग करे सबकुछ आसान है, कम से कम IIT JEE Maths में आसानी से FULL Marks आसकते है. Maths by SUHAAG; Join करे में हनत करे, सफलता प्राप्त करे --- Thanks ALL THE BEST  
-10/2/2013 form SUHAAG.